Risk assessment of high-speed railway CTC system based on improved game theory and cloud model

Yanhao Sun, Tao Zhang, Shuxin Ding and Zhiming Yuan

Signal and Communication Research Institute, China Academy of Railway Sciences Corporation Limited, Beijing, China and Traffic Management Laboratory for High-Speed Railway, National Engineering Research Center of System Technology for High-Speed Railway and Urban Rail Transit, Beijing, China, and Shengliang Yang

Signal and Telecommunication Department, China Railway Chengdu Group Company Limited, Chengdu, China and Postgraduate Department, China Academy of Railway Sciences, Beijing, China

Abstract

Purpose – In order to solve the problem of inaccurate calculation of index weights, subjectivity and uncertainty of index assessment in the risk assessment process, this study aims to propose a scientific and reasonable centralized traffic control (CTC) system risk assessment method.

Design/methodology/approach – First, system-theoretic process analysis (STPA) is used to conduct risk analysis on the CTC system and constructs risk assessment indexes based on this analysis. Then, to enhance the accuracy of weight calculation, the fuzzy analytical hierarchy process (FAHP), fuzzy decision-making trial and evaluation laboratory (FDEMATEL) and entropy weight method are employed to calculate the subjective weight, relative weight and objective weight of each index. These three types of weights are combined using game theory to obtain the combined weight for each index. To reduce subjectivity and uncertainty in the assessment process, the backward cloud generator method is utilized to obtain the numerical character (NC) of the cloud model for each index. The NCs of the indexes are then weighted to derive the comprehensive cloud for risk assessment of the CTC system. This cloud model is used to obtain the CTC system’s comprehensive risk assessment. The model’s similarity measurement method gauges the likeness between the comprehensive risk assessment cloud and the risk standard cloud. Finally, this process yields the risk assessment results for the CTC system.

Findings – The cloud model can handle the subjectivity and fuzziness in the risk assessment process well. The cloud model-based risk assessment method was applied to the CTC system risk assessment of a railway group and achieved good results.

Originality/value – This study provides a cloud model-based method for risk assessment of CTC systems, which accurately calculates the weight of risk indexes and uses cloud models to reduce uncertainty and
subjectivity in the assessment, achieving effective risk assessment of CTC systems. It can provide a reference and theoretical basis for risk management of the CTC system.

**Keywords** High-speed railway, Centralized traffic control, Risk assessment, Game theory, Cloud model

**Paper type** Research paper

1. **Introduction**

With the continuous development of China’s economy, High-speed railway (HSR) has become the main body of inter-regional rapid transportation in the comprehensive transportation system (Song, Gao, Li, Liu, & Dong, 2023). The HSR dispatching system is the brain and nerve center of the HSR transportation system and plays a huge role in ensuring the safety, punctuality, and efficient operation of HSR trains (Sun, Zhang, Yuan, Gao, & Ding, 2020). With the continuous advancement of science and technology, China HSR dispatching system is based on the Centralized Traffic Control (CTC), realizing the automation and remote control of dispatching and command centered on train operation plan control. The CTC system is mainly composed of three parts: the railway administration central subsystem, the station subsystem, and the network subsystem (Ding, Zhang, Sheng, Chen, & Yuan, 2023), which are highly coupled. If the risks between these subsystems are not handled properly, it may cause CTC system disorder and affect train operating efficiency. In severe cases, it may even lead to major accidents (Zhang et al., 2022). For example, the 2008 Chatsworth train collision in the United States, the 2012 Buenos Aires rail disaster in Argentina, and the 2020 Livraga derailment in Italy indicate potential risk issues with the CTC systems (Xu et al., 2023). Therefore, it becomes an important issue for CTC system developers to focus on improving the safety of the CTC systems. Risk assessment has a strong guiding role in identifying the risks of the CTC systems and reducing accidents. Therefore, it is necessary to study the risk assessment of the CTC systems.

Safety is the eternal theme and the lifeline of railway transportation (Zhang, Li, Yuan, & Yu, 2018). Therefore, many experts and scholars have conducted risk assessments on the development of railway systems and have achieved certain research results. By collecting various accident reports and holding workshops with railway safety experts, Leitner (2017) identified various hazardous events that may directly lead to casualties. And a risk assessment was conducted on the Slovakian railway system by using safety technologies such as Fault Tree Analysis (FTA) technology and Event Tree Analysis (ETA) technology. Alawad, Kaewunruen, and An (2020) proposed a novel framework that uses computer vision and pattern recognition to perform risk management in railway systems (Hwang & Jo, 2013). first used the Preliminary Hazard Analysis (PHA) method to draw the initial hazard sources at the most fundamental stage, and then used Hazard and Operability Study (HAZOP) to evaluate the risks of the railway signaling system. Szacíkło, Krześniak, Jasiński, and Valls (2022) used the traditional risk matrix assessment method to assess rail freight transport risks. In order to apply it, the causes and consequences of undesirable events during the implementation of rail freight transport were specified. (Zhang, Xu, & Su, 2013) combined Failure Mode, Effects and Criticality Analysis (FMECA) and Fuzzy Analytical Hierarchy Process (FAHP) to construct a new risk assessment method. Finally, a case study on risk assessment of the interval signal control function for the train control center (TCC) is used to illustrate the application of the proposed risk assessment method. Iczuk and Kyeko (2023) used the Failure Mode and Effect Analysis (FMEA) method and the fuzzy set method, as well as various methods of fuzzification and defuzzification. In order to overcome the inherent imprecision and uncertainty of the available data, Jafarian and Rezvani (2012) improved FTA using fuzzy sets and extended the minimal cut-set and the Fussell–Vesely importance measures of the conventional approach into the fuzzy environment. Considering both existing expertise and uncertainties, such as fuzziness and randomness of the evaluation, Wu, Zhen, and Zhang (2020) evaluated urban rail transit operation safety through the Criterion Relevance (CRITIC) method based on the cloud model.
and improved criterion importance. Cases were used to prove that the modified method can indeed conduct a scientific, systematic, and objective evaluation of the index system.

The above experts and scholars have provided significant insights into risk assessment. For example, how to deal with fuzziness in risk assessment, calculate the weight of risk factors, etc. For the fuzziness of risk assessment, some experts used fuzzy sets to deal with it, and some experts use cloud models to deal with it. Compared with fuzzy sets, cloud models can better handle the conversion of qualitative data into quantitative concepts. Therefore, using cloud models for risk assessment has become a trend (Zhang, Wu, Chen, Skibniewski, & Zhong, 2015). Another issue in risk assessment is obtaining the weights of risk factors or risk indexes. In the aforementioned research regarding the acquisition of weights, some use the FAHP, while others use the CRITIC. However, these two methods can only obtain subjective weights or objective weights separately. There is relatively few research on combining these two types of weights. Even in cases where studies do combine them, it is often a simple linear combination. As belongs to the operation research theory, game theory can better coordinate the conflicts between different weighting methods, maximizes the mutual benefits of various weighting methods, and obtains the most satisfying combined weight (Wu, Lee, Guizani, & Wang, 2014). Therefore, this paper aims to propose a risk assessment model for the HSR CTC systems, which is based on cloud model theory and uses game theory to obtain the combined weight of risk indexes.

The remainder of this paper is displayed as follows. Section 2 briefly introduces the CTC system and conducts risk analysis on the CTC system using System-Theoretic Process Analysis (STPA), laying the foundation for subsequent CTC system risk assessment. Section 3 introduces three methods of calculating weights and a weight combination calculation method based on game theory. In addition, a brief introduction to the cloud model theory was given, and the risk assessment steps based on the cloud model were given. Section 4 is an example of verifying the method in this article and conducts a risk assessment on the CTC system of a railway administration. Section 5 summarizes this paper and points out the direction for next research.

2. CTC system risk analysis
The CTC system is a telecontrol system divided into two levels: the central system and the station system. Dispatchers located in the railway administration's dispatch center complete operations such as plan adjustments, route control, and issuance of dispatch orders through various terminal devices in the CTC center system. The operation instruction information is sent to the train service terminal or station autonomous machine of the corresponding station through the communication machine. The station attendant operates the train service terminal to accept the plan issued by the CTC center and sign for the dispatch order. The station autonomous machine generates instructions according to the adjustment plan and sends them to the computer-based interlocking (CBI) system for execution. The station receipt information for the plan and dispatching commands is back to the dispatch center through the communication machine program. The station operation terminal can also directly send instructions to the station autonomous machine. In addition to the internal information exchange of the CTC system, the CTC system also communicates with external systems such as radio block center (RBC), temporary speed restriction server (TSRS), CBI, and TCC through system interfaces for information transmission and feedback. Obviously, the CTC system is a typical control-feedback system.

Regarding risk analysis of complex systems, the most classic and commonly used models are the system-theoretic accident model and process (STAMP) and the STPA based on STAMP (Leveson, 2004). Different from commonly used linear chain-of-events models, such as hazard and operability analysis, FMEA and FTA, etc. STPA considers the interaction between components or the hazards involving non-failure of components (Sülaman, Beer, Felderer, & Höst, 2019). STPA starts with identifying types of potential losses of the target
system, hazards for those losses, and constraints for the hazards. Then, create a STAMP model for the system, that is, a control structure composed of control actions and feedback between the controller and the controlled process. Next, identify the potential unsafe control actions (UCA) for each control action in the control structure that could result in system hazards and losses. Finally, determine how each UCA occurs and how it propagates to system losses (loss scenario). The analysis process of STPA is shown in Figure 1.

The steps for conducting risk analysis on the CTC system using STPA are as follows.

**Step 1**: Define possible losses and hazards in the CTC system. The following three losses and eight hazards are defined according to the functions of the CTC system, as shown in Table 1 and Table 2, respectively.

**Step 2**: Define the CTC system control structure. Based on the functions of the CTC system and the information flow of its interaction with other systems, the control structure of the CTC system is established. The control structure of the CTC system is shown in Figure 2.

**Step 3**: Identify the UCA of the CTC system. Considering the constraints of space, this paper takes the interaction between the dispatcher and the CTC system as an example for illustration, as shown in Table 3.

**Step 4**: Determine how each UCA occurs. The possible causes of UCA and the loss scenario caused by UCA are shown in Table 4.

### 3. Methodology

#### 3.1 Combined weight calculation method based on game theory

The acquisition of index weights is crucial for risk assessment, and its accuracy directly impacts the risk evaluation results. The consideration of weights is mostly focused on subjective or objective data. The combined weight calculation method based on game theory is used to calculate the weights of risk factors, which can better reflect the importance of different factors. The specific calculation process is shown in the following steps:

1. **Define System Level Hazards and Constraints**: Identify the potential hazards and constraints in the system.
2. **Model Control Structure**: Establish the control structure of the system, including the controller and the controlled process.
3. **Identify Unsafe Control Actions (UCA)**: Determine the UCA that could result in system hazards and losses.
4. **Identify Loss Scenarios**: Understand how each UCA occurs and how it propagates to system losses.

### Table 1.

<table>
<thead>
<tr>
<th>Loss ID</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>L-1</td>
<td>Train reception and departure accidents</td>
</tr>
<tr>
<td>L-2</td>
<td>Shunting operation accident</td>
</tr>
<tr>
<td>L-3</td>
<td>Railway external casualty accident</td>
</tr>
</tbody>
</table>

**Source(s):** Authors’ own work
objective weights. However, there is relatively less emphasis on correlation weights. From the perspective of information theory, if one index significantly influences another, indicating that the former provides more information than the latter, and it should be assigned a higher weight. Therefore, calculating correlation weights for indexes is also reasonable.

3.1.1 Calculation of subjective weights. Analytical Hierarchy Process (AHP) is a classical method for calculating subjective weights, but in constructing the judgment matrix, it is challenging for experts or decision-makers to make precise pairwise comparisons among indexes. In order to overcome this problem, this paper uses triangular fuzzy numbers (TFN) to improve AHP.

Definition 1. If $Q$ is a TNF, then it can be represented as:

$$Q = (x, \mu(x)) | x \in X$$

(1)

where $X$ represents the range of values for the input variable $x$, and $\mu(x)$ is the membership degree of $x$, with its membership function as:

$$\mu(x) = \begin{cases} 
0 & \text{otherwise} \\
\frac{x - a}{b - a} & a \leq x < b \\
\frac{c - x}{c - b} & b \leq x < c
\end{cases}$$

(2)

As shown in Figure 3, $a$, $b$, and $c$ are the lower, median, and upper bounds of the TNF, respectively.

Definition 2. Let $Q_1 = (a_1, b_1, c_1)$ and $Q_2 = (a_2, b_2, c_2)$ be two TNFs, then the degree of possibility of $Q_1 \geq Q_2$ is defined as $V(Q_1 \geq Q_2)$, and it can be also expressed as:

$$V(Q_1 \geq Q_2) = \begin{cases} 
1 & b_1 \geq b_2 \\
\frac{(a_2 - c_1)}{(b_1 - c_1)(b_2 - a_2)} & b_1 \leq b_2, a_2 \leq c_1 \\
0 & \text{other}
\end{cases}$$

(3)
Primary dispatcher operation
Assistant dispatcher operation
CTC Application Server
Station Autonomous Machine
Station Operation Terminal
Wireless Train Number Verification System
Radio Block Center
GSM-R Interface Server
Temporary Speed Restriction Server

Dispatcher
Information receipt
Route instruction information;
Alarm information;
Report time point information;
Dispatching order receipt

Assistant dispatcher operation
Manual modification instructions;
Manual triggering instructions;
Manually handling train routes;
Issue dispatching order

CTC Application Server
Train status information;
Connection state information;
Emergency stop command;
Related operation feedback information

Radio Block Center
Feedback order results;
Speed limit command status;

GSM-R Interface Server
Train control speed limit interface;
Temporary speed limit order

Temporary Speed Restriction Server
Train control speed limit interface;
Temporary speed limit order

Source(s): Authors’ own work
The simple steps are as follows.

Step 1: According to Table 5, use the TNF to compare $n$ indexes pairwise and construct a fuzzy judgment matrix $Q$.

$$ Q = (Q_{ij})_{n \times n} = (a_{ij}, b_{ij}, c_{ij})_{n \times n} \quad (4) $$

Step 2: Calculate the fuzzy relative weights of the $j$-th index with respect to other indexes.

$$ S_j = \left[ \begin{array}{ccc} \frac{\sum_{i=1}^{n} a_{ij}}{\sum_{i=1}^{n} a_{ij}}, \frac{\sum_{i=1}^{n} b_{ij}}{\sum_{i=1}^{n} b_{ij}}, \frac{\sum_{i=1}^{n} c_{ij}}{\sum_{i=1}^{n} c_{ij}} \end{array} \right] \quad (5) $$

Step 3: According to the calculation degree of possibility in Equation (3), the possibility of the $j$-th index compared to other indexes is calculated:

<table>
<thead>
<tr>
<th>Control action</th>
<th>Uncontrol</th>
<th>Control</th>
<th>Control at the wrong time</th>
<th>Stop too soon/Applying too long</th>
</tr>
</thead>
<tbody>
<tr>
<td>Dispatcher modifies instructions</td>
<td>The dispatcher did not modify the instructions, causing hazards H-1 and H-2</td>
<td>The dispatcher modified the instruction, causing hazard H3</td>
<td>The dispatcher modified the instructions at the wrong time, causing hazards H1, H2, and H3</td>
<td>N/A</td>
</tr>
<tr>
<td>Dispatcher executes instructions</td>
<td>The dispatcher failed to execute the instructions, causing hazards H-1 and H-2</td>
<td>The dispatcher executed the instruction, causing hazard H3</td>
<td>The dispatcher executed the instructions at the wrong time, causing hazards H1, H2, and H3</td>
<td>N/A</td>
</tr>
<tr>
<td>Dispatcher handles the train route</td>
<td>The dispatcher failed to handle the approach, causing hazards H1 and H2</td>
<td>The dispatcher handled the train route, causing danger H3</td>
<td>The dispatcher handled the train route at the wrong time, causing hazards H1, H2, and H3</td>
<td>N/A</td>
</tr>
<tr>
<td>Dispatcher sends dispatch orders</td>
<td>The dispatcher did not send dispatching orders, causing dangers H1 and H2</td>
<td>The dispatcher sends a dispatch command, causing danger H3</td>
<td>The dispatcher sends dispatching commands at the wrong time, causing hazards H1, H2, and H3</td>
<td>N/A</td>
</tr>
<tr>
<td>Dispatcher issues train operation adjustment plans</td>
<td>The dispatcher did not issue the train operation adjustment plan, causing hazards H1 and H2</td>
<td>The dispatcher issues the train operation adjustment plan, causing hazard H3</td>
<td>The dispatcher issues the train operation adjustment plan at the wrong time, causing hazards H1, H2, and H3</td>
<td>N/A</td>
</tr>
<tr>
<td>Dispatcher sends train operation voucher</td>
<td>The dispatcher failed to send the train operation voucher, causing hazards H1 and H2</td>
<td>The dispatcher sends the train operation voucher, causing hazards H3</td>
<td>The dispatcher sends the train operation voucher at the wrong time, causing hazards H1, H2, and H3</td>
<td>N/A</td>
</tr>
</tbody>
</table>

Source(s): Authors’ own work

Table 3. UCA between the dispatcher and CTC system

High-speed railway CTC system risk assessment
\( d(Q_i) = \min_{i,j=1,2,\ldots,n \land i \neq j} V(Q_i \geq Q_j) \)  

Step 4: Normalize \( d(Q_i) \) to obtain the subjective weights of the indexes.

\[
W_S = \left[ \frac{d(Q_1)}{\sum_{j=1}^{n} d(Q_j)}, \frac{d(Q_2)}{\sum_{j=1}^{n} d(Q_j)}, \ldots, \frac{d(Q_n)}{\sum_{j=1}^{n} d(Q_j)} \right] 
\]

**Table 4.** The causes and consequences of UCA

<table>
<thead>
<tr>
<th>UCA</th>
<th>Possible cause</th>
<th>Loss scenario</th>
</tr>
</thead>
</table>
| The dispatcher did not modify the instructions | The shunting work order issued to the locomotive did not receive a receipt in time  
The wireless shunting route arrangement application information sent by the driver to the autonomous machine was not received  
The train operation adjustment plan is being implemented, but the adjustment time calculated by the autonomous calculation has not yet started | H-1 or H-2    |
| The dispatcher modified the instructions | Received wrong receipt information  
The wireless shunting route arrangement application information received from the driver to the autonomous machine is incorrect | H-3           |
| Dispatchers modify instructions when they make mistakes | The shunting work order sent to the locomotive has not received a receipt  
The wireless shunting application information sent by the driver to the autonomous machine was not received in time  
During the execution of the train operation adjustment plan, the shunting time calculated by the autonomous machine was wrong  
The successive route resulted in the operating time of various trains not being implemented according to the standard time | H-1 or H-2 or H-3 |

**Note(s):** “...” indicates that the table is not fully displayed. Due to the space limit of the paper, only a part of the table has been intercepted. **Source(s):** Authors’ own work
3.1.2 Calculation of relative weights. The interrelationship between indexes has a significant impact on the weights of the indexes. Therefore, for risk assessment, relative weights also need to be calculated. Decision-making Trial and Evaluation Laboratory (DEMATEL) is a comprehensive method for building and analyzing a structural model involving causal relationships between complex factors. However, it is also subjective. Similar to AHP, DEMATEL can be enhanced by using TNF to calculate the relative weights of indexes. The steps of the Fuzzy Decision-making Trial and Evaluation Laboratory (FDEMATEL) are as follows:

Step 1: According to Table 5, a fuzzy initial direct-relation matrix $B$ is constructed using TNF to represent the degree of mutual influence among $n$ indexes.

$$P = (P_{ij})_{n \times n} = (a_{ij}, b_{ij}, c_{ij})_{n \times n}$$  \hspace{1cm} (8)

Step 2: The Converting Fuzzy data into Crisp Scores (CFCS) method is used to defuzzify $P$ to obtain the direct-relation matrix $D$ (Zhang et al., 2015). Then, calculate the standard direct influence matrix, standardize the direct influence matrix $D$ according to Equation (9), and obtain the standardized direct-relation matrix $G$.

$$G = [g_{ij}]_{n \times n} = \min \left( \frac{1}{\max \sum_{j=1}^{n} d_{ij}}, \frac{1}{\max \sum_{i=1}^{n} d_{ij}} \right) D$$  \hspace{1cm} (9)

Step 3: Calculate the total relation matrix $T$. The calculation equation is as follows.

$$T = [t_{ij}]_{n \times n} = G(E - G)^{-1}$$  \hspace{1cm} (10)

where $E$ represents the identity matrix.

Step 4: Calculate the relevance of indexes $r_j$.

$$r_j = \sum_{j=1}^{n} t_{ij} - \sum_{i=1}^{n} t_{ij}$$  \hspace{1cm} (11)

The greater the relevance of an index, the greater its impact on other indexes. In the context of risk assessment, higher relevance indicates greater risk, and consequently, the weight assigned to it is also higher. Normalize the relevance to obtain the correlation weight of the index.

<table>
<thead>
<tr>
<th>Importance</th>
<th>Influence</th>
<th>TNF$(a, b, c)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Equally important</td>
<td>No influence</td>
<td>(0.0, 0.1, 0.3)</td>
</tr>
<tr>
<td>Slightly important</td>
<td>Low influence</td>
<td>(0.1, 0.3, 0.5)</td>
</tr>
<tr>
<td>Important</td>
<td>Medium influence</td>
<td>(0.3, 0.5, 0.7)</td>
</tr>
<tr>
<td>Very important</td>
<td>High influence</td>
<td>(0.5, 0.7, 0.9)</td>
</tr>
<tr>
<td>Extremely important</td>
<td>Very high influence</td>
<td>(0.7, 0.9, 1)</td>
</tr>
</tbody>
</table>

Source(s): Authors’ own work

Table 5. The correspondence between TNF and importance & influence
3.1.3 Calculation of objective weights. The basic steps of the entropy weight method are as follows (Yuan, Li, Xu, Zhao, & Liu, 2019).

**Step 1**: Establish risk assessment matrix $Y$ composed of $m$ evaluation experts and $n$ evaluation indexes.

\[
Y = [y_{ij}]_{m \times n}
\]  

(13)

**Step 2**: If the indexes have the benefit index or the cost index, then the benefit index is normalized according to Equation (14), and the cost-type index is normalized according to Equation (15):

\[
z_{ij} = \frac{y_{ij} - \min(v_{ij})}{\max_j(y_{ij}) - \min_j(y_{ij})} \tag{14}
\]

\[
z_{ij} = \frac{\max_j(y_{ij}) - y_{ij}}{\max_j(y_{ij}) - \min_j(y_{ij})} \tag{15}
\]

**Step 3**: According to the definition of entropy in the information theory, the information entropy of the $j$-th evaluation index is:

\[
e_j = -\frac{1}{\ln n} \sum_{j=1}^{n} v_{ij} \ln v_{ij} \tag{16}
\]

where $v_{ij} = \frac{v_{ij}}{\sum_j v_{ij}}$, if $v_{ij} = 0$, then define $\ln v_{ij} = 0$.

**Step 4**: Calculate the weight of the index based on information entropy.

\[
W_O = \left[ \frac{1 - e_1}{n - \sum_{j=1}^{n} e_j}, \frac{1 - e_2}{n - \sum_{j=1}^{n} e_j}, \ldots, \frac{1 - e_n}{n - \sum_{j=1}^{n} e_j} \right] \tag{17}
\]

3.1.4 Combined weights based on game theory. Compared with the general linear combined method, the combined weight method based on game theory can better balance the differences between different weight calculation methods, making the acquisition of combined weight more reasonable and accurate (Xie et al., 2022).

Assuming that the index weights $W_k, (k = 1, 2, \ldots, L)$ are obtained through $L$ methods, these weights are then subject to arbitrary linear combinations.
\[ W = \sum_{k=1}^{L} \alpha_k W_k^T \]  

where \( \alpha_k \) is the coefficient for the linear combination, and \( \alpha_k > 0 \).

Based on game theory, seek the most satisfied \( W^* \) in the possible vector sets and the most satisfied weight coefficient \( \alpha_k \) to minimize the deviation between \( W^* \) and \( W_k \).

\[
\min \left\| \sum_{k=1}^{L} \alpha_k W_k^T - W_j \right\| \quad k = 1, 2, \ldots, L
\]

(19)

According to the differential properties of the matrix, the first derivative of Equation (20) is transformed into a system of linear equations.

\[
\begin{bmatrix}
W_1 W_1^T & W_1 W_2^T & \cdots & W_1 W_L^T \\
W_2 W_1^T & W_2 W_2^T & \cdots & \vdots \\
\vdots & \vdots & \ddots & \vdots \\
W_L W_1^T & W_L W_2^T & \cdots & W_L W_L^T
\end{bmatrix}
\begin{bmatrix}
\alpha_1 \\
\alpha_2 \\
\vdots \\
\alpha_L
\end{bmatrix}
= 
\begin{bmatrix}
W_1 W_1^T \\
W_2 W_2^T \\
\vdots \\
W_L W_L^T
\end{bmatrix}
\]

(20)

Normalize \([\alpha_1, \alpha_2, \ldots, \alpha_L]\).

\[
\alpha_k^* = \frac{\alpha_k}{\sum_{k=1}^{L} \alpha_k}
\]

(21)

Finally, the optimal combined weight is obtained.

\[
W^* = \sum_{k=1}^{L} \alpha_k^* W_k^T
\]

(22)

3.2 Cloud model theory

In 1995, Academician Li Deyi proposed the cloud model theory based on probability theory and fuzzy set theory. This model can implement the uncertain transformation between a qualitative concept and its quantitative instantiations quantitative aspects, effectively overcoming uncertainty issues in conventional risk assessments (He & Liu, 2020).

3.2.1 Basic concepts of cloud model. Let \( U \) be a domain of discourse represented by quantitative values and \( C \) be the qualitative concept on \( U \). If the qualitative value is \( x \in U \) and \( x \) is a random implementation of the qualitative concept \( C \), the certainty degree \( U(x) \in [0, 1] \) of \( x \) with regard to \( C \) is the random number with a steady tendency (Wu et al., 2014), that is,

\[
\mu: U \rightarrow [0, 1], \forall x \in U, x \rightarrow \mu(x)
\]

(23)

Then, the distribution of \( x \) on the domain \( U \) is called a cloud, and each \((x, \mu(x))\) is called a cloud droplet. Cloud models can be divided into triangular clouds, rectangular clouds, trapezoidal clouds, and normal clouds, according to the different shapes of clouds. In the real
world, since a large number of random phenomena generally obey normal distribution, this paper adopts the normal cloud distribution model as the modeling object. In this paper, the term "cloud model" specifically refers to the normal cloud model.

3.2.2 The numerical character of cloud model. The numerical character (NC) of the cloud is represented by three values: expectation $E_x$, entropy $E_n$, and hyper entropy $H_e$, which are recorded as $C(E_x, E_n, H_e)$. The expectation $E_x$ represents the distribution expectation of cloud droplets in the domain space, reflecting the points in the domain space that can best represent qualitative concepts. The entropy $E_n$ represents the degree of determinism of qualitative concepts, reflecting the size of the range of values that the domain space can be accepted by qualitative concepts. The hyper entropy $H_e$ represents the determinism measure of entropy, reflecting the degree of dispersion of cloud droplets (Wang, Wang, Wang, Au-Yong, & Ali, 2021). Figure 4 is an example of a cloud model with $E_x = 0.5$, $E_n = 0.2$, $H_e = 0.015$, and cloud drop number $N$ is set as 4000.

There are two methods for determining the NC of cloud mode: one is the backward cloud generator method, which is mainly used to generate NC for index evaluation. This method is based on statistical principles, transforming data into NC $C(E_x, E_n, H_e)$ representing qualitative concepts of clouds, and then forming a normal cloud. The algorithm steps are as follows.

**Input:** $M$ experts’ assessment of risk indexes $x_i (i = 1, 2, ..., M)$.

**Output:** Cloud model NC $C(E_x, E_n, H_e)$ of evaluation indexes.

Firstly, Calculate the sample mean, which is the expectation $E_x$.

$$E_x = \bar{x} = \frac{1}{M} \sum_{i=1}^{1} x_i$$  \hspace{1cm} (24)

Next, calculate the sample variance.

![Cloud model diagram](image_url)

**Source(s):** Authors’ own work
Finally, calculate the entropy \( E_n \) and hyper entropy \( H_e \).

\[
E_n = \sqrt{\frac{\pi}{2} \sum_{i=1}^{M} |x_i - Ex|}
\]

\[
H_e = \sqrt{S^2 - E_n^2}
\]

Another NC generation method is mainly used to generate the NC of the assessment standard cloud, that is, the NC that determines the assessment level. Suppose the left boundary of each level scoring interval of the assessment index is \( C_{\min} \) and the right boundary is \( C_{\max} \). Then, the cloud model NC is determined using Equation (28).

\[
\begin{align*}
Ex &= (C_{\max} + C_{\min}) / 2 \\
E_n &= (C_{\max} - C_{\min}) / 6 \\
H_e &= \eta
\end{align*}
\]

where \( \eta \) is a constant that can be adjusted according to the fuzzy threshold of the variable. Its value is generally determined by experience and can be adjusted according to the actual situation.

3.2.3 Cloud model similarity measurement. Similarity measurement can be performed between two different cloud models. The traditional method is to use the expectation \( Ex \) as the benchmark. Although this method is simple, it does not take into account the two NC of \( E_n \) and \( H_e \), so the results of the similarity measurement are rough.

In order to calculate the similarity measure of cloud models more accurately, the paper proposes a cloud model similarity measurement method based on the improved expectation curve and Kullback-Leibler (KL) divergence.

If the cloud droplet \( x \) satisfies \( x \sim N(Ex, En^2) \), \( En \neq 0 \), \( En' \sim N(En, He^2) \), then

\[
y(x) = \exp \left( -\frac{(x - Ex)^2}{2(En^2 + He^2)} \right)
\]

where \( y(x) \) is called the modified expectation curve of a normal cloud (Gong, Jiang, & Liang, 2015).

KL divergence is an asymmetry measure of the difference between two probability density functions (PDF). It is often used to measure the difference between two PDFs. The greater the KL divergence, the greater the difference between the two PDFs (Budka, Gabrys, & Musial, 2011).

This paper uses KL divergence to measure the difference in the modified expectation curves of two cloud models, thereby measuring the similarity of the two cloud models. For continuous random variables \( P \) and \( Q \), their PDFs are \( p(x) \) and \( q(x) \), respectively, and the KL divergence is defined as follows.

\[
D_{KL}(P \parallel Q) = \int p(x) \log \frac{p(x)}{q(x)} dx
\]

There is a symmetrical form of KL divergence, namely \( D(P \parallel Q) = D_{KL}(Q \parallel P) + D_{KL}(P \parallel Q) \) (Xu & Wang, 2014). Combined with the improved expectation curve, the
difference calculation formula of the two cloud models \( C_1(Ex_1, En_1, He_1) \) and \( C_2(Ex_2, En_2, He_2) \) can be derived as follows (Yang, Qin, & Su, 2022).

\[
D(C_1, C_2) = \frac{1}{2} \left[ (Ex_1 - Ex_2)^2 + (\sigma_1^2 + \sigma_2^2) \right] \times \left( \frac{1}{\sigma_1^2 + \sigma_2^2} \right) - 2 \tag{31}
\]

where \( \sigma_1^2 = En_1^2 + He_1^2 \), \( \sigma_2^2 = En_2^2 + He_2^2 \). According to the difference \( (C_1, C_2) \), the similarity measurement formula for cloud models is defined as.

\[
Sim(C_1, C_2) = \exp(-D(C_1, C_2)) \tag{32}
\]

### 3.3 Risk assessment method based on improved game theory and cloud model

#### 3.3.1 Building the risk assessment indexes for the CTC system

The STPA method was utilized to conduct a risk analysis of the CTC system and establish risk assessment indexes for it. These indexes are divided into two levels: the first level comprises three indexes, while the second level consists of 12 indexes, as illustrated in Figure 5.

**Figure 5.** The CTC system risk assessment indexes

**Source(s):** Authors’ own work
3.3.2 Obtain the cloud model NC of risk assessment index and standard. Assume that \( M \) experts evaluate the risk indexes of the CTC system, and the expert’s evaluation result is \( x_i (i = 1, 2, ..., M) \). Calculate the NC of the cloud model for the risk index based on Equations (24) ~ (27).

For the assessment standard, use the natural optimal golden section model to determine the score interval and standard cloud model parameters within the scoring interval \([0,1]\), then obtain the NC of the assessment standard cloud according to Equation (28), as depicted in Table 6.

Generating a standard assessment cloud map through the cloud NC of the standard assessment, as shown in Figure 6.

3.3.3 Generate CTC system comprehensive assessment cloud. After obtaining the NC of the risk assessment index, and considering the different weights assigned to each index, it is necessary to perform a weighted aggregation operation on the NC of the index assessment to obtain the final comprehensive assessment cloud.

<table>
<thead>
<tr>
<th>Risk level</th>
<th>Score interval</th>
<th>NC</th>
<th>Risk description</th>
</tr>
</thead>
<tbody>
<tr>
<td>I High Risk</td>
<td>[0.691, 1]</td>
<td>(1,0.103,0.0131)</td>
<td>The CTC system has basically lost all its functions and is extremely prone to major accidents and casualties</td>
</tr>
<tr>
<td>II Slightly High Risk</td>
<td>[0.499,0.883]</td>
<td>(0.691,0.064,0.0081)</td>
<td>The CTC system risk has reached a critical level, and certain improvement measures must be implemented for the risk</td>
</tr>
<tr>
<td>III High Risk</td>
<td>[0.407,0.593]</td>
<td>(0.500,0.031,0.0050)</td>
<td>The CTC system has the risk of reduced system performance and reduced transportation efficiency</td>
</tr>
<tr>
<td>IV Medium Risk</td>
<td>[0.117,0.501]</td>
<td>(0.309,0.064,0.0081)</td>
<td>The CTC system operates well, risks in the system can be dealt with in a timely manner, and the main functions of the system can be realized</td>
</tr>
<tr>
<td>Slightly Low Risk</td>
<td>[0.117,0.501]</td>
<td>(0.309,0.064,0.0081)</td>
<td>The CTC system operates well, risks in the system can be dealt with in a timely manner, and the main functions of the system can be realized</td>
</tr>
</tbody>
</table>

Source(s): Authors’ own work

Table 6. The NC of the assessment standard cloud

Figure 6. The standard assessment cloud map

Source(s): Authors’ own work
RS

Assuming there are $N$ assessment indexes, the NC of the index is $C(Ex_j, En_j, He_j)$, ($j = 1, 2, ..., N$), and the weight of the index are $w_j$. The formula for the weighted operation of the NC is as follows (Zhou, Zhang, Guo, & Zhao, 2020):

$$
Ex = \frac{\sum_{j=1}^{N} Ex_j \times En_j \times w_j}{\sum_{j=1}^{N} En_j \times w_j},
En = \sum_{j=1}^{N} En_j \times w_j,
He = \frac{\sum_{j=1}^{N} He_j \times En_j \times w_j}{\sum_{j=1}^{N} En_j \times w_j}
$$

(33)

Based on the NC of the comprehensive assessment cloud, draw the comprehensive assessment cloud diagram. Next, utilize the cloud model measurement method to measure the similarity between the comprehensive assessment cloud and the standard assessment cloud. Finally, obtain the risk assessment results. See Figure 7.

**Figure 7.**
The risk assessment process flowchart of the CTC system

Source(s): Authors’ own work
4. Case study
In order to enhance the safety and reliability of the CTC system and reduce system risks, a railway group invited 10 experts, 10 train dispatchers, and 10 station attendants to conduct a risk assessment on the CTC system of a railway line. The assessment score interval is [0, 1]. The larger the score, the higher the risk of the index. According to Equations (24) ~ (27), use the backward cloud generator method to convert the score data provided by the experts into the NC of the risk index, as shown in Table 7.

According to Equations (4) ~ (17), the subjective weight, relative weight and objective weight of the index are calculated respectively. Next, use Equations (18) ~ (22) to calculate the combined weight of the index. The weights of the first-level index are shown in Table 8, and the weights of the second-level index are shown in Table 9.

After obtaining the index weights, use Equation (33) to perform a weighted calculation on the NC of the second-level index risk assessment cloud model to obtain the NC of the first-level index risk assessment cloud model, as illustrated in Table 10. Subsequently, generate their respective cloud maps based on the NC of the second-level index, which is shown in Figure 8–10. Similarly, the NC of the first-level indexes risk assessment cloud model is obtained. The NC is weighted and calculated to obtain the NC of the CTC system risk assessment cloud model, which is \( E_X = 0.342, E_N = 0.072, H_e = 0.015 \). Finally, a comprehensive CTC system risk assessment cloud map is generated, shown in Figure 11.

<table>
<thead>
<tr>
<th>Second level index</th>
<th>Subjective weight</th>
<th>Relative weight</th>
<th>Objective weight</th>
<th>Combined weight</th>
</tr>
</thead>
<tbody>
<tr>
<td>Alarm information of CTC system</td>
<td>0.356</td>
<td>0.058</td>
<td>0.009</td>
<td></td>
</tr>
<tr>
<td>The usability of CTC system</td>
<td>0.391</td>
<td>0.140</td>
<td>0.017</td>
<td></td>
</tr>
<tr>
<td>The interface display of CTC system</td>
<td>0.293</td>
<td>0.097</td>
<td>0.013</td>
<td></td>
</tr>
<tr>
<td>Interface information exchange between the CTC system and RBC</td>
<td>0.317</td>
<td>0.034</td>
<td>0.009</td>
<td></td>
</tr>
<tr>
<td>Interface information exchange between the CTC system and TSRS</td>
<td>0.350</td>
<td>0.030</td>
<td>0.012</td>
<td></td>
</tr>
<tr>
<td>Interface information exchange between the CTC system and CBI</td>
<td>0.361</td>
<td>0.067</td>
<td>0.008</td>
<td></td>
</tr>
<tr>
<td>Interface information exchange between the CTC system and TCC</td>
<td>0.250</td>
<td>0.035</td>
<td>0.005</td>
<td></td>
</tr>
<tr>
<td>Interface information exchange between the CTC system and GSM-R</td>
<td>0.247</td>
<td>0.081</td>
<td>0.031</td>
<td></td>
</tr>
<tr>
<td>Maintenance and updates of the CTC system</td>
<td>0.337</td>
<td>0.030</td>
<td>0.017</td>
<td></td>
</tr>
<tr>
<td>Reliability of CTC system equipment</td>
<td>0.349</td>
<td>0.032</td>
<td>0.023</td>
<td></td>
</tr>
<tr>
<td>CTC system software reliability</td>
<td>0.203</td>
<td>0.037</td>
<td>0.015</td>
<td></td>
</tr>
<tr>
<td>Internal information exchange within CTC system</td>
<td>0.339</td>
<td>0.053</td>
<td>0.015</td>
<td></td>
</tr>
</tbody>
</table>

Source(s): Authors' own work

<table>
<thead>
<tr>
<th>First level index</th>
<th>Subjective weigh</th>
<th>Relative weigh</th>
<th>Objective weight</th>
<th>Combined weight</th>
</tr>
</thead>
<tbody>
<tr>
<td>The human-machine interface of CTC system</td>
<td>0.336</td>
<td>0.458</td>
<td>0.408</td>
<td>0.44</td>
</tr>
<tr>
<td>Information exchange between CTC system and external systems</td>
<td>0.243</td>
<td>0.321</td>
<td>0.279</td>
<td>0.258</td>
</tr>
<tr>
<td>Reliability of CTC system</td>
<td>0.421</td>
<td>0.221</td>
<td>0.313</td>
<td>0.302</td>
</tr>
</tbody>
</table>

Source(s): Authors' own work

Table 7. The NC of the second-level index
Table 8. Weights of the first-level index
It is obvious that although the cloud maps in Figure 8–11 are between the risk level III and risk level IV, they are more inclined to the risk level IV. In order to make the results more convincing, the similarity measurement between the evaluation cloud and the standard cloud was calculated according to Equations (30) ~ (32), and the results are shown in Table 11.

Through the calculation of the similarity measurement, it can be seen that both the three first-level indexes and the final CTC system risk assessment results are more biased toward risk level IV, that is, the CTC system is running well, risks in the system can be dealt with in a timely manner, and the system is the main functions can be realized. Comparing the assessment results of the risk assessment method based on fuzzy evidential reasoning proposed by Wei, Xu, and Zhang (2020) and the results based on the causative Bayesian network proposed by (Chen, Li, Wang, Wang, & Qiu, 2023), all three methods show risk assessment results at level IV. This suggests that the risk assessment method proposed in this paper is effective.

<table>
<thead>
<tr>
<th>Second level index</th>
<th>Subjective weight</th>
<th>Relative weight</th>
<th>Objective weight</th>
<th>Combined weight</th>
</tr>
</thead>
<tbody>
<tr>
<td>Alarm information of CTC system</td>
<td>0.292</td>
<td>0.221</td>
<td>0.295</td>
<td>0.270</td>
</tr>
<tr>
<td>The usability of CTC system</td>
<td>0.353</td>
<td>0.438</td>
<td>0.495</td>
<td>0.432</td>
</tr>
<tr>
<td>The interface display of CTC system</td>
<td>0.373</td>
<td>0.341</td>
<td>0.210</td>
<td>0.298</td>
</tr>
<tr>
<td>Interface information exchange between the CTC system and RBC</td>
<td>0.225</td>
<td>0.227</td>
<td>0.143</td>
<td>0.197</td>
</tr>
<tr>
<td>Interface information exchange between the CTC system and TSRS</td>
<td>0.126</td>
<td>0.260</td>
<td>0.119</td>
<td>0.175</td>
</tr>
<tr>
<td>Interface information exchange between the CTC system and CBI</td>
<td>0.359</td>
<td>0.282</td>
<td>0.244</td>
<td>0.288</td>
</tr>
<tr>
<td>Interface information exchange between the CTC system and TCC</td>
<td>0.176</td>
<td>0.141</td>
<td>0.256</td>
<td>0.191</td>
</tr>
<tr>
<td>Interface information exchange between the CTC system and GSM-R</td>
<td>0.114</td>
<td>0.09</td>
<td>0.238</td>
<td>0.149</td>
</tr>
<tr>
<td>Maintenance and updates of the CTC system</td>
<td>0.169</td>
<td>0.120</td>
<td>0.168</td>
<td>0.153</td>
</tr>
<tr>
<td>Reliability of CTC system equipment</td>
<td>0.267</td>
<td>0.376</td>
<td>0.294</td>
<td>0.313</td>
</tr>
<tr>
<td>CTC system software reliability</td>
<td>0.326</td>
<td>0.193</td>
<td>0.310</td>
<td>0.277</td>
</tr>
<tr>
<td>Internal information exchange within CTC system</td>
<td>0.238</td>
<td>0.311</td>
<td>0.228</td>
<td>0.257</td>
</tr>
</tbody>
</table>

Table 9. The weights of the second-level index

Source(s): Authors’ own work

<table>
<thead>
<tr>
<th>First level index</th>
<th>Ex</th>
<th>NC</th>
<th>En</th>
<th>He</th>
</tr>
</thead>
<tbody>
<tr>
<td>Alarm information of CTC system</td>
<td>0.358</td>
<td>0.105</td>
<td>0.015</td>
<td></td>
</tr>
<tr>
<td>The usability of CTC system</td>
<td>0.222</td>
<td>0.057</td>
<td>0.013</td>
<td></td>
</tr>
<tr>
<td>The interface display of CTC system</td>
<td>0.306</td>
<td>0.039</td>
<td>0.017</td>
<td></td>
</tr>
</tbody>
</table>

Table 10. The NC of the first-level index

Source(s): Authors’ own work
High-speed railway CTC system risk assessment

Figure 8. The cloud map of the human-machine interface of CTC system

Source(s): Authors' own work

Figure 9. The cloud map of information exchange between CTC system and external systems

Source(s): Authors' own work
Figure 10. The cloud map of reliability of CTC system

Source(s): Authors' own work

Figure 11. The comprehensive cloud map of CTC system risk assessment

Source(s): Authors' own work
5. Conclusion

The HSR CTC system is crucial to ensuring the driving safety of high-speed railway trains, and risk assessment is an important means of safety management. Considering the fuzziness and difficulty of quantifying risks, this paper proposes a cloud model-based risk assessment method for CTC systems. Furthermore, this method was used to conduct a risk assessment on the CTC system of a certain railway administration, achieving good application results and providing relatively actual system risk assessment results. The main conclusions are:

(1) STPA was used to conduct risk analysis on the CTC system, and a two-level risk index system was constructed for the CTC system. The proposed index system can cover the risk attributes of the CTC system effectively and lays the foundation for the risk assessment of the CTC system.

(2) The weight of the risk index is significant for the calculation of risk assessment. The combined weight calculation method based on game theory overcomes the shortcomings of the low accuracy of a single weight calculation method.

(3) The cloud model can overcome shortcomings such as fuzziness and difficulty in quantification in the risk assessment process. Compared with a single numerical assessment, the assessment results are more intuitive. The effectiveness of the method was verified by conducting a risk assessment on the CTC system of a certain railway administration, which can provide theoretical and methodological support for risk assessment of the CTC system.

(4) The backward cloud generator method in this paper exhibits some errors in hyper-entropy estimation when the sample size is small. Therefore, future research will focus on enhancing the reverse cloud algorithm to improve the accuracy of the evaluation results.

References


Corresponding author
Zhiming Yuan can be contacted at: zhimingyuan@hotmail.com